## Strength and fracture properties of asbestos-cement mortar composites

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The strength and fracture properties of random asbestos fibre-reinforced cement mortar composites are reported in this paper. The fibre content varies between 5% and 20% by weight. Both the ultimate tensile strength ( $\sigma_t$ ) and the modulus of rupture ( $\sigma_b$ ) increase with increasing fibre-volume fraction. These results are shown to agree satisfactorily with the law of mixtures modified for randomly oriented short fibre-reinforced composites. The critical stress intensity factor ( $K_c$ ) and the specific work of fracture (R) have been determined using three-point bend edge-notched beams and grooved double-cantileverbeam (DCB) specimens. There is generally good agreement between these two physical quantities estimated from the two testpiece geometries. It is shown that the fibre pull-out mechanism is dominant in the fracture of asbestos cements and that the specific work of fracture can be reasonably well predicted by considering the energies absorbed in both the pull-out and the fibre/matrix interfacial debonding processes.

#### 1. Introduction

Asbestos cement is a composite material made up the new polyamide fibre, Kevlar, is probably the of short asbestos fibres randomly dispersed in a most promising substitute fibre to give efficient recement mortar matrix. It is widely used in the inforcement for cementitious matrices. Good building industry for making fire-proofing and composite strength (similar to asbestos cements) insulating materials, sewer pipes, corrugated and and high impact toughness (approximately tenflat sheets for roof covering and wall lining. In fold increase) have been obtained in these Kevlarsuch applications it is necessary that the as- cement composites [4]. bestos cement products possess an acceptable bending strength and propagation.

fibres it is apparent that prices will eventually properties similar to asbestos cements. This choice become uneconomical to justify their use for cannot be properly made until we have a complete reinforcement of cements. Thus there is a need to understanding of the independent properties of search for a suitable substitute fibre for cement the cement mortar matrix, the asbestos fibres, the reinforcement. The use of glass fibres, carbon fibre/matrix interface and fibres and organic polymeric filaments such as mechanisms for the asbestos cement composites. polypropylene and nylon as suitable substitute Aveston [5] and Martin and Phillips [6] have fibres has been studied by Majumdar and considerably advanced our knowledge of the co-workers [1-3]. It is found that to obtain physical texture and mechanical strength of the both good impact resistance and high bend- asbestos fibres. Walsh et al. [7] and Birchall et al ing strength a mixture of organic and inorganic [8] have provided detailed explanations for fibres is needed in the cement [1]. Recently, the brittle strength of cements. However, in 0022-2461/79/092091-12 \$03.20/0 © 1979 Chapman and Hall Ltd.

Walton and Majumdar [4] have demonstrated that

basic considerations The for good a resistance to crack replacement fibre are that it shall produce a resultant composite which possesses strength, With the continuing demand for asbestos crack resistance and other mechanical and physical the reinforcing

relation to composites, apart from the early preliminary study of Allen [9], it appears that there has not been any systematic work on the strength and fracture properties of asbestos cements published in the open literature. Information on the interfacial properties including the bonding nature of asbestos fibres to cement mortar matrices and on the source of fracture toughness in such asbestos cement composites is particularly lacking at present. This paper only deals with the latter problem to elucidate the fracture mechanisms of asbestos cements and is not concerned with the fibre/cement matrix interface problem which is the subject of a future investigation. It will be shown (in Section 4.2) that the fibre pull-out process constitutes the major contribution to the total fracture resistance of asbestos cements. The effects of asbestos fibre-volume fraction on the tensile strength, modulus of rupture and specific work of fracture have been investigated in this paper.

#### 2. Theoretical considerations

# 2.1. Strength of asbestos cement composites

The law of mixtures for aligned continuous fibrous composites may be modified to predict the strength of asbestos cements. It will be assumed that at failure the asbestos fibres are not broken but are pulled out of the cement matrix.\* Thus the average tensile stress in the fibre  $(\sigma_f)$  is given by

$$\sigma_{\mathbf{f}} = 2\tau(l/d) \tag{1}$$

where  $\tau$  is the fibre-matrix interfacial bond strength, l and d are the length and diameter of the asbestos fibre. With random orientation of the short fibres, only those which are parallel or nearly parallel to the loading direction can produce efficient reinforcement. For fibres which are less favourably oriented full reinforcement will not be achieved and an efficiency factor must be applied. By assuming uniform distribution of fibres in the matrix, Romualdi and Mandel [10] have shown that the effective fibre-volume fraction is 41% of the nominal volume fraction if the fibres can be orientated in any direction with equal probability. It is therefore possible to rewrite the ultimate tensile strength  $(\sigma_t)$  equation for the asbestos cement composite as:

$$\sigma_{\rm t} = \sigma_{\rm m} v_{\rm m} + 0.41 \,\sigma_{\rm f} v_{\rm f}, \qquad (2)$$

where  $\sigma_{\rm m}$  is the tensile strength of the unreinforced cement mortar matrix and  $v_{\rm m}$ ,  $v_{\rm f}$  are the volume fractions of the matrix and the asbestos fibres, respectively. This is reduced to

$$\sigma_{\mathbf{t}} = \sigma_{\mathbf{m}} v_{\mathbf{m}} + 0.82\tau v_{\mathbf{f}}(l/d) \tag{3}$$

using Equation 1 for  $\sigma_f$ . Equation 3 may be extended to predict the modulus of rupture  $(\sigma_b)$  of asbestos cements since in general we have  $\sigma_b = \alpha \sigma_t$  and  $\sigma_{m,b} = \beta \sigma_m$ , where  $\alpha, \beta$  are constants which can be determined from experiments and  $\sigma_{m,b}$  is the modulus of rupture of the cement mortar matrix in bending. Thus,

$$\sigma_{\mathbf{b}} = \left(\frac{\alpha}{\beta}\right) \sigma_{\mathbf{mb}} v_{\mathbf{m}} + 0.82(\alpha \tau) v_{\mathbf{f}}(l/d). \quad (4)$$

Equations 3 and 4 were first given by Swamy and Mangat [11] for concrete reinforced with randomly distributed short steel fibres.

## 2.2. Critical stress intensity factor and specific work of fracture of asbestos cement composites

Linear elastic fracture mechanics concepts were first applied by Kaplan [12] to concrete and subsequently extended to cement paste, mortar and random short fibre-reinforced concrete by others [13–16]. Fracture parameters such as the critical stress intensity factor  $(K_c)$  and the critical strain energy release rate  $(G_c)$  have been studied by a number of different methods. Although linear elastic fracture mechanics is strictly speaking inapplicable for these materials which are microscopically heterogenous and anisotropic, the success of using toughness parameters as fracture criteria has been clearly demonstrated by experimental results which indicate that  $EG_{c} \simeq K_{c}^{2}$ where  $G_{c}$  and  $K_{c}$  are measured independently. Of course, for this relationship to hold, the pseudo plastic zone size and any inelastic effects at the crack tip must be small. It should be noted that both  $K_c$  and  $G_c$  correspond to fracture initiation values and where no slow crack growth occurs they become fracture instability values. It is expected that this linear elastic fracture mechanics approach will be applicable to asbestos cements. Mindess et al. [17] recently have suggested the use of the J-integral [18] to give a more realistic fracture parameter for fibre-reinforced concrete.  $J_{\rm c}$ , which is the critical J value at crack initiation can be experimentally determined using one deep

\* This assumption is justified since microscopic examination of fracture surfaces show little sign of fibre breakage. 2092 edge-notched and one unnotched specimen subjected to bending [17]. It will be shown that for the asbestos cements studied in this work the load-deflection curve is linear to the point of crack propagation. Thus, for this linear elastic situation,

$$J_{\rm c} = G_{\rm c} \simeq K_{\rm c}^2 / E, \qquad (5)$$

so that the *J*-integral approach and the  $K_c$  or  $G_c$  analysis are equivalent.

The work of fracture method [19] has also been used to measure the specific fracture resistance\* (R) of fibre-reinforced composites using three-point bend notched specimens. R is given by (see Fig. 1)

$$R = \frac{U}{B(W-a)} \tag{6}$$

where U is the integrated area under the loaddeflection curve which includes both the crack initiation  $(U_i)$  and crack propagation  $(U_p)$  energies, B is the specimen thickness, W is the width and a is the notch depth. R is usually not a constant (especially for strain-rate sensitive materials) and decreases with increasing a/W. To determine valid values of R it is necessary that crack propagation is stable and continuous, otherwise if unstable cracking occurs, the specific work of fracture estimated from the saw-tooth load—deformation curve is an upper bound value. It is also possible to define a crack-initiation resistance parameter  $(R_i)$  by

$$R_{\rm i} = \frac{U_{\rm i}}{B(W-a)}.$$
 (7)

This initiation value assumes that all  $U_i$  is released for crack propagation over the ligament area B(W-a) and is thus identical to  $J_c$ ,  $G_c$  and  $K_c^2/E$ 



as described previously. Unlike R,  $R_i$  is independent of a/W for fibrous composite materials [20].

The work of fracture method [19] suffers two limitations in its usefulness for the determination of R. Firstly cracking is normally unstable unless a/W is relatively large. The a/W ratio at which stable cracking commences depends on the asbestos fibre volume fraction. Secondly even if cracking is stable, only one R value is obtained per specimen. Gurney and Hunt [21] have developed a quasi-static crack propagation technique which is suitable for the determination of specific work of fracture (R) of asbestos cements in specimens where crack propagation is stable and where there is no irreversible deformation at regions remote from the crack tip. An appropriate specimen such as the double-cantilever-beam (DCB) configuration may be used conveniently with the Gurney method to yield several R measurements per testpiece. For asbestos cements R is expected to increase with crack length (in DCB specimens) since more and more fibres that bridge the crack opening are being pulled out as the crack advances. Patterson and Chan [22] have demonstrated the general validity of the Gurney approach for Rmeasurements in glass fibre-reinforced cements.

## 2.3. Source of fracture toughness of asbestos cements

A generalized theory has been proposed by Marston *et al.* [23] where the specific fracture resistance (*R*) is given by the sum of the separate toughnesses resulting from fibre pull-out ( $R_{po}$ ), redistribution of stresses ( $R_{re}$ ) and fracture of surfaces ( $R_s$ ). For the asbestos cements studied here the average fibre length (*l*) is less than the critical transfer length ( $l_c$ ) (see Section 4.1) and it seems, therefore, appropriate to neglect  $R_{re}$  as a component contribution to the specific work of fracture (*R*). Thus

$$R = R_{\rm po} + R_{\rm s} \tag{8}$$

where for  $l < l_c$ , so that fracture of fibres does not occur,

$$R_{\mathbf{po}} = \frac{0.41 \, v_{\mathbf{f}} l^2 \tau}{6d} \tag{9}$$

Figure 1 Schematic diagram for R determination by the work of fracture method.

 $R_{\rm s} = v_{\rm m} R_{\rm m} + (0.41 v_{\rm f}) \frac{4 \,\overline{l} R_{\rm if}}{d}.$  (10)

\*Usually the symbol  $(2\gamma)$  is used for R by other research workers. It measures the average fracture energy per unit crack area over the entire fracture process.

and

 $l(\simeq l/4)$  is the average pull-out length of the asbestos fibres and  $R_m$ ,  $R_{if}$  are the fracture energies of the cement mortar matrix, and fibre-matrix interface, respectively. Since Equations 9 and 10 are originally derived for composites with aligned fibres and since the effective volume fraction of reinforcement is less than the nominal  $v_{\rm f}$  in random fibre composites, an effeciency factor of 0.41 (the same as that used in Equation 2) is applied to these toughness expressions. Harris et al. [14] have adopted a similar correction procedure when analysing the fracture toughness of randomly distributed short steel fibre-reinforced concrete. They have, however, used an experimentally determined value of 0.55 instead of 0.41 because the fibre distribution is not fully random in three dimensions in their material. In the absence of independent data for  $R_{if}$ , an upper bound is given by  $R_{if} \simeq R_m$ [23] so that Equation 10 is simplified to

$$R_{\rm s} \simeq 0.41 v_{\rm f} \frac{lR_{\rm m}}{d} + v_{\rm m} R_{\rm m}. \qquad (11)$$

The specific work of fracture (R) is thus given by

$$R = \frac{0.41 v_{\rm f} l^2 \tau}{6d} + \left[ v_{\rm m} + 0.41 \frac{v_{\rm f} l}{d} \right] R_{\rm m}.$$
(12)

#### 3. Experimental work

### 3.1. Material

The asbestos fibre-reinforced cement mortar composites with fibre mass fractions of 5% to 20% were supplied by James Hardie & Coy Pty Ltd. The asbestos was initially fiberized (i.e. split down to fine fibres) by four passes through a laboratory mill which gave the properties shown in Table I before mixing with the silica-cement slurry, Table II gives the composition and the calculated fibre volume fractions of the four formulations of asbestos cements studied in this work. The castings were made in a vacuum filter box approximately 190 mm square.\* After curing for 24 h at 100% r.h. they were autoclaved at 0.86 MPa for 8h. Specimens for strength and fracture tests were then cut on a diamond saw to specified dimensions. For the fracture toughness specimens the last 3 to 4 mm of the required crack length was cut by a blade 0.15 mm thick.

TABLE I Characterization of asbestos fibres

(1) Bauer-McNett classification			
Material retained on sieve (%)	Test 1	Test 2	
4 mesh	32.8	35.0	
14 mesh	20.4	17.0	
35 mesh	15.4	13.6	
200 mesh	12.2	11.6	
Through 200 mesh (by difference)	19.2	22.8	
(2) T. & N. elutriator			
Material retained (%)	Test 1	Test 2	
Crude	1.6	2.4	
Partly opened	10.4	11.2	
Open	72.0	71.2	
Through 200 mesh (by difference)	16.0	15.2	
(3) Dyckerhoff air permeability test Surface area: 1128 m <sup>2</sup> kg <sup>-1</sup>			

## 3.2. Specimen geometries and test procedure

Rectangular strips measuring 6 mm were used for tensile strength and three-point bending flexural strength tests conducted in a Hounsfield Tensometer and an Instron testing machine. The Young's modulus in tension  $(E_t)$  was measured using an Instron extensometer and that in bending  $(E_b)$  was calculated from the slope of the load-deflection curve taking into consideration the compliance of the testing machine.

Both three-point bend edge-notched (Fig. 1) and grooved double-cantilever-beam (DCB) (Fig. 2) specimens were used for fracture toughness testing. Equations 6 and 7 show how  $R_i$  and R are determined from the three-point bend notched beam test results using the work of fracture method. The critical stress intensity factor  $(K_c)$  is given by either (see Fig. 1)

$$K_{\mathbf{c}} = \frac{1.5P_{\mathbf{i}}La^{1/2}}{BW^2} \times [1.93 - 3.07(a/W) + 14.53(a/W)^2 - 25.11(a/W)^3 + 25.8(a/W)^4] \quad (13)$$

following Brown and Srawley [24] or by

$$K_{c} = \frac{1.5P_{i}L}{B(W-a)^{3/2}} \left[Y(a/W)\right]^{1/2} \quad (14)$$

<sup>\*</sup>The specimens prepared from these castings are thus different from the normal commercially manufactured products which have a laminated structure. Mechanical properties determined for these asbestos cements are, therefore, not necessarily representative of commercial products.

ΤA	B	L	E	II	Compo	sition	of	asbestos	cement
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Formulation no.	Raw materials (wt %)	<b>.</b>	Composite density	Fibre volume	
	Cassiar AK asbestos $(m_{\rm f}) \times 10^2$	Cement	Ground silica	$\rho_{\rm c}  (\rm kg  m^{-3})$	fraction (v <sub>f</sub> )
1	5	57	38	1550	0.030
2	10	44	36	1420	0.056
3	15	51	34	1390	0.082
4	20	48	32	1350	0.106

N.B. Density of Cassiar AK asbestos ( $\rho_{\rm f}$ )  $\simeq 2550$  kg m<sup>-3</sup> and  $v_{\rm f} = m_{\rm f} (\rho_{\rm c}/\rho_{\rm f})$ .

after Winne and Wundt [25], where Y is a geometric correction factor and  $P_i$  is the load at crack. initiation.\* The difference between these two Kexpressions is no more than 8% for  $a/W \le 0.6$  and only Equation 13 is used here to calculate  $K_c$  for the present three-point bend notched specimens.

For the DCB specimens the specific work of fracture (R) was determined using Gurney's graphical irreversible work area method as briefly outlined in Fig. 2.  $K_c$  may also be determined for this testpiece geometry if the fracture initiation load  $(P_i)$  and the instantaneous crack length  $(a_i)$  can be simultaneously recorded. Thus,

$$K_{\rm c} = \frac{3.46P_{\rm i}(a_{\rm i}/H + 0.7)}{\sqrt{(BB_{\rm n}H)}}$$
(15)



Figure 2 Illustration of the quasi-static crack propagation technique to determine R.

\*In the present experiments  $P_i$  corresponds to the maximum load.

where  $B_n$  is the net section thickness and *H* is the height of one cantilever beam.

## 4. Results and discussion

## 4.1. Strength results

The ultimate tensile strength ( $\sigma_t$ ) and the modulus of rupture  $(\sigma_{\mathbf{b}})$  results are shown in Figs. 3 and 4 respectively. Both  $\sigma_{\mathbf{b}}$  and  $\sigma_{\mathbf{t}}$  increase with increasing mass fraction of asbestos fibres  $(m_f)$  with  $\sigma_b$ levelling out at  $m_f = 0.15$ . It should be noted that the  $\sigma_b$  results shown in Fig. 4 contain two sets of data, one obtained by loading in the beam thickness direction and the other in the beam width direction. The good agreement between these experimental data suggests that the distribution of fibres within the cement mortar matrix is fully random. To use Equations 3 and 4 to predict  $\sigma_t$  and  $\sigma_h$ , it is necessary to determine the corresponding values of  $\alpha$ ,  $\beta$ ,  $\tau$  and the fibre aspect ratio (l/d). By back-extrapolation to  $m_f = 0$  in Figs. 3 and 4,  $\sigma_m$  (= 3 MPa) and  $\sigma_{mb}$  (= 10 MPa) can be obtained for the unreinforced cement mortar matrix. Thus  $\beta (= \sigma_{mb} / \sigma_m) = 3.3$  Dividing  $\sigma_{\rm b}$  with  $\sigma_{\rm t}$  for all the four formulations of asbestos cements and averaging these values gives  $\alpha = 2.69$ . Exact values of l and d for the fibres are difficult to measure since these depend on the degree of fiberization and on the milling process in which the fibres are separated into different grades by length classifiers (see Table I). Moreover, the fibres are usually bundled together (Figs. 5a and b) and they may spread open after being pulled out from the matrix (Fig. 5c). Since it is the fibre bundles that provide the reinforcement for the cement matrix, l and d measurements must therefore correspond to the fibre bundles and not the individual fibres. Both  $\overline{l}$  and d were measured directly from SEM pictures taken on fracture surfaces of broken specimens. Thus the average fibre-bundle diameter (d) is approximately 25  $\mu$ m and the average pullout fibre length  $(\overline{l})$  is 1 mm so that  $l (= 4\overline{l})$  is



Figure 3 Variation of ultimate tensile strength with mass fraction of asbestos. Bars indicate 1 standard deviation and sample size = 10.



Figure 4 Variation of modulus of rupture with mass fraction of asbestos. Bars indicate 1 standard deviation and sample size = 10.

and

4 mm. The pull-out stress ( $\tau$ ) for Chrysotile fibres in a cement matrix as quoted by de Vekey and Majumdar [26] is 0.83 MPa. Using these values of l, d and  $\tau$  in conjunction with Equation 1, the critical transfer length ( $l_c$ ) for the fibres becomes 45 mm, assuming  $\sigma_f = 3$  GPa. Therefore, the assumption of fibre pull-out in deriving the strength and toughness equations in Section 2 is justified since  $l_c > l$  as calculated above. The ultimate tensile strength and the modulus of rupture equations can now be rewritten as:

$$\sigma_{\rm t} = 3v_{\rm m} + 108.9v_{\rm f}$$
 (MPa) (16)

$$\sigma_{\rm b} = 8.2v_{\rm m} + 292.9v_{\rm f}$$
 (MPa) (17)

where the relationship between  $v_f$  and  $m_f$  and their corresponding values are given in Table II. As shown in Figs. 3 and 4 the dashed lines predicted by Equations 16 and 17 are in reasonable agreement with experimental results. This is considered satisfactory since the maximum error is only about 18%. In fact, much better agreement between



Figure 5 (a) A fibre bundle after pull-out showing cement mortar debris on fibre ( $\times$  1200). (b) A fibre bundle showing base near cement mortar matrix '(X 700). (c) Opening of individual fibres of a bundle after pull-out (× 250).

theory and experiment is obtained if  $\tau = 1$  MPa is used in the calculations.

bestos fibres.\* This behaviour is rather different from the results obtained by Allen [9] where  $E_t$ decreases almost linearly with increasing  $v_{\rm f}$ . This is probably a consequence of the fact that the asbestos cements used in [9] are manufactured differently to the composites used in this work. In particular, unlike the present asbestos cements, those used by Allen have unusually large matrix void contents  $(v_{0})$  which are found to increase significantly from 14% to 60% when  $v_{\rm f}$  is increased from 4% to 15%. Thus his  $E_t$  values must decrease with  $v_{\rm f}$  because the increase in stiffness by addition of fibres is more than offset by the reduction of the matrix stiffness due to these sharply increasing matrix voids [9]. The present results show that  $E_t$  is approximately twice  $E_b$ , an observation which has also been recently reported for Kevlar cement composites cured by autoclaving [4].

## 4.2. Fracture toughness results 4.2.1. Three-point bend edge-notched beam results

Fig. 7 shows a set of typical load-deflection curves for the notched beams under three-point bending. For shallow notch depths cracking was unstable. However, crack stability was improved as the notch depth was increased. It is possible to calculate  $K_{c}$ ,  $R_{i}$  and R using these graphical records and Equations 13, 7 and 6, respectively. Figs. 8 to 10 show the variation of  $K_c$ ,  $R_i$  and R with (a/W) for the four asbestos cement composites. As expected all these fracture parameters increase with increasing volume fraction of asbestos fibres (see Fig. 11). There is apparently no improvement in  $R_i$  and R beyond  $m_f = 0.15$ . The exact reason for this behaviour is presently unknown. There is not much difference in appearance of the fracture surfaces for  $m_f = 0.15$  and 0.20, except perhaps for the latter there seems to be slightly more voids in the matrix. It is possible that, as a result of this, the toughness contribution by the creation of new surfaces will be reduced and the effective interfacial bond strength diminished if such voids are located close to the fibres. Also for these large Fig. 6 shows that the average Young's moduli fibre volume fraction composites interactions beof the asbestos cements in bending and in direct tween fibres will tend to decrease the efficiency of tension are independent of the mass fraction of as- reinforcement. All these factors added together

\*Because of the small  $E_f/E_m$  and the large l/d ratios,  $E_t$ , as calculated from the rule of mixtures modified for random oriented short fibres, is essentially constant over the whole range of  $v_f$  studied. Thus  $E_t$  is approximately 19 GPa, since  $E_{f} = 70 \text{ GPa} \text{ and } E_{m} = 20 \text{ GPa}.$ 



Figure 6 Variation of Young's modulus in bending and in direct tension with mass fraction of asbestos fibres.



Figure 7 Load/deflection curves for asbestos cement composites with  $m_f = 0.15$  and different notch depth ratios (a/W).

may have offset the predicted increase in toughness (i.e. Equation 12) with  $v_{\rm f}$  beyond 15% mass fraction of fibres. It is obvious that much more serious work is needed to show exactly why additions of fibres beyond  $m_{\rm f} = 0.15$  does not bring about further increases in strength and toughness. In broad terms both  $K_{\rm c}$  and  $R_{\rm i}$  are in-

dependent of a/W. By equating  $K_c^2 = E_b R_i$ ,  $E_b$  can be predicted using these two fracture mechanics parameters. These results are superimposed in Fig. 6 and they agree reasonably well with corresponding measured  $E_b$  values. The specific work of fracture (R) (including the crack initiation and propagation energies), however, decreases with



Figures 9 and 10 Variation of specific work of fracture (R) and specific crack initiation energy ( $R_i$ ) with notch depth ratio (a/W) for asbestos cements with different mass fractions of fibres (three-point bend edge-notched specimens).

a/W and tends to level out at  $a/W \ge 0.4$ . It should be noted that R has obviously been over-estimated at small a/W where cracking is unstable.

 $J_c$  for the asbestos cements were calculated using the following equation [27]:

$$J_{\rm c} = \frac{2}{B(W-a)} \int_0^{\delta_{\rm crack}} P {\rm d}\delta_{\rm crack} \qquad (18)$$

i.e. 
$$J_{\rm c} = \frac{2}{B(W-a)} (U_{\rm i} - U_0)$$
 (18a)

where  $U_i$  and  $U_0$  are respective areas under the  $P-\delta$  curves for the notched and unnotched beams integrated to the fracture-initiation load of the notched beam. Table III shows that  $J_c$  agrees fairly well with  $R_i$  for all the asbestos cements.



TABLE III  $J_c$  and  $R_i$  results for asbestos cements using three-point bend notched beams

Sample	$m_{\mathbf{f}}$	a/W	J <sub>c</sub> (kJ m <sup>-2</sup>	$R_{i}$ (kJ m <sup>-2</sup> )
1-7e	0.05	0.51	0.34	0.43
1-7f	0.05	0.55	0.35	0.47
2–7e	0.10	0.55	1.51	1.43
2–7f	0.10	0.56	1.50	1.50
3–7d	0.15	0.56	1.23	1.70
3–7e	0.15	0.57	1.80	1.80
4–7e	0.20	0.54	1.58	2.00
4–7f	0.20	0.54	1.95	2.20

## 4.2.2. Double-cantilever-beam specimen results

Fig. 12 shows a typical load-deflection curve for quasi-static cracking in a grooved DCB specimen. Cracking was in general stable, as would be anticipated for this specimen geometry made from a material with constant R [28]. However, there were a few cases where the grooves were not deep enough to constrain the crack from veering out of the arms. Figs. 13 and 14 show the variation of Ras the crack length increases. Only those data obtained from specimens with a straight crack are included in these plots. The increase of R with increasing a/W may be simply explained by the fact that fibres bridging the gap and behind the crack front are also pulled-out as the crack advances. The starting a/W for these DCB specimens were approximately 0.30, and at this initial crack length the R values for the different asbestos cements were close to the corresponding  $R_i$  values obtained from three-point bend notched specimens. It should also be pointed out that the upper and

Figure 11 Variation of  $K_c$  and  $R_i$  with mass fraction of asbestos fibres. Bars indicate 1 standard deviation.



Figure 12 Load-deflection curve for quasi-static crack propagation in a DCB specimen with  $m_f = 0.20$  and  $B_n = 4.02$  mm.

lower bound R values derived from these two specimen geometries are consistent although the trends of R varying with a/W are exactly opposite. The decreasing trend of R with a/W for the threepoint bend notched specimens is thought to be associated with increasing control of crack growth and hence decreasing kinetic energy losses as the notch depth increases [29]. In the DCB specimens cracking is quasi-static so that kinetic energy losses are negligible.

Equation 15 has also been used to calculate  $K_c$  for the DCB specimens. As shown in Table IV these  $K_c$  results agree very well with corresponding values derived from three-point bend notched beams. This indicates that  $K_c$  is a usable material parameter for the asbestos-cement composites.\*

\*Recent experimental  $K_c$  results obtained from large single-edge-notched (SEN) specimens [30] compare favourably with corresponding values derived from these DCB and three-point bend notched specimens.



Figures 13 and 14 Variation of R with non-dimensional crack length (a/W) for different asbestos cements (DCB specimens).

Asbestos content	DCB specimens		Three-point bend notched beams		
$(m_{\rm f})$	$\overline{K_{\rm c}}$ (MPa $\sqrt{\rm m}$ )	Sample size	$K_{c}$ (MPa $\sqrt{m}$ )	Sample size	
0.05	1.74 ± 0.31*	5	1.53 ± 0.17*	11	
0.10	$2.52 \pm 0.27$	9	$2.34 \pm 0.18$	8	
0.15	$3.38 \pm 0.34$	8	$3.25 \pm 0.38$	8	
0.20	3.66 ± 0.24	9	3.44 ± 0.29	8	

TABLE IV Comparison of  $K_c$  in DCB specimens and three-point bend notched beams

\*1 standard deviation.

## 4.2.3. Prediction of fracture toughness of asbestos cements

Fig. 15 shows a typical fracture surface of the asbestos cements where the fibre pull-out mechanism is clearly displayed.  $R_s$  and  $R_{po}$  have been calculated using Equations 11 and 9 and the following values:  $l = 4 \text{ mm}, d = 25 \mu \text{m}, \tau = 0.83 \text{ MPa}$ and  $R_{\rm m} = R_{\rm if} = 20 \, {\rm J \, m^{-2}}$  (by back-extrapolation of the  $R_i$  curve in Fig. 11 to  $m_f = 0$ ). Table V shows that the predicted R-values  $(=R_s + R_{po})$ in reasonably are good agreement with corresponding experimental fracture toughness results obtained from DCB specimens. Since  $R_{po} \gg R_s$  the source of fracture toughness of asbestos cement mortar composites is predominantly due to the fibre pull-out process. The energies absorbed in creating new surfaces matrix and interface debonding - contribute only

approximately 5% of the total specific fracture work.



Figure 15 A typical SEM fracture surface of an asbestos cement ( $m_{\rm f} = 0.15$ ) showing the predominant fibre pullout mechanism ( $\times$  35).

TABLE V Prediction of fracture toughness in asbestos cements.

$m_{\mathbf{f}}$	$v_{\mathbf{f}}$	$R_{\rm s}$ (kJ m <sup>2</sup> )	$R_{po}(kJ m^{-2})$	$R_{\rm s} + R_{\rm po} (\rm kJ  m^{-2})$	<i>R</i> (kJ m <sup>-2</sup> )
0.05	0.030	0.06	1.09	1.15	$0.92 \pm 0.28*(n^{\dagger} = 10)$
0.10	0.56	0.09	2.03	2.12	$1.60 \pm 0.60 (n = 18)$
0.15	0.082	0.12	2.98	3.10	$2.92 \pm 0.68 \ (n = 24)$
0.20	0.106	0.15	3.85	4.00	$3.37 \pm 0.80 \ (n = 24)$

 $^{\dagger}n$  = sample size of experimental data obtained in DCB specimens.

\*1 standard deviation.

### 5. Conclusions

The strength and fracture properties of asbestos cement mortar composites with  $m_f$  between 0.05 to 0.20 have been studied in this paper. It is found that the modified law of mixtures strength Equations 3 and 4 give fairly good agreement in  $\sigma_t$ and  $\sigma_{\rm b}$  with experimental results. The critical stress intensity factor  $(K_c)$  and the specific crackinitiation energy  $(R_i)$  measured from DCB specimens and three-point bend edge-notched testpieces are consistent with one another and may therefore be regarded as usable material properties. The specific work of fracture (including both initiation and propagation energies) (R) is shown to increase with increasing crack length in DCB specimens, owing to fibres bridging the crack tips. R-values for the asbestos cement composites can be reasonably well predicted by considering the energies absorbed in both the fibre pull-out and the fibre-matrix interface debonding processes. The fibre pull-out mechanism contributes more than 95% of the total fracture work and is thus the major source of fracture toughness in the asbestos cements.

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